

Q-3 **Attempt all questions** (14)

a) Discuss the consistency of the system of equation (5)

$$2x + 3y + 4z = 11, x + 5y + 7z = 15, 3x + 11y + 13z = 25.$$

If it is consistent then find it's solution.

b) Find characteristic equation of matrix (5)

$$\begin{bmatrix} 2 & 1 & 1 \\ 0 & 1 & 0 \\ 1 & 1 & 2 \end{bmatrix}. \text{ Using it find value of}$$

$$A^8 - 5A^7 + 7A^6 - 3A^5 + A^4 - 5A^3 + 8A^2 - 2A + I$$

c) If $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ then verify Caley Hamilton's theorem. (4)

Q-4 **Attempt all questions** (14)

a) Solve: $(x^2 - y^2)dx + 2xy dy = 0$. (5)

b) Solve: $\frac{dy}{dx} = \cos x \cos y - \sin x \sin y$. (5)

c) Solve: $\frac{dy}{dx} + \frac{4x}{x^2+1} y = \frac{1}{(x^2+1)^3}$. (4)

Q-5 **Attempt all questions** (14)

a) Find equation of sphere which passes through $(0,0,0)$, $(2,0,0)$, $(0,3,0)$ and $(0,0,4)$. (5)

b) Find equation of sphere having end points of diameter are $(1, -2, 3)$ and $(0, -1, 3)$. (5)

c) Write the polar form of the following points : (4)

$$(a) (1, \sqrt{3}) \quad (b) (-\pi\sqrt{2}, \pi\sqrt{2})$$

Q-6 **Attempt all questions** (14)

a) State and prove Leibnitz's theorem for n^{th} derivative of product. (6)

b) Find n^{th} derivative of the following : (4)

$$(a) \frac{1}{(x-1)(x+2)} \quad (b) \frac{x}{x^2-1}$$

c) If $y = \cos(m\sin^{-1}(x))$ then show that $(1-x^2)y_{n+1} - x(2n+1)y_{n+1} + (m^2-n^2)y_n=0$. (4)

Q-7 **Attempt all questions** (14)

a) State and prove machlaurin's series of e^x also deduce the machlaurin's series of $\cosh x$. (5)

b) Find Taylor's series of $x^5 + 4x^4 + 6x^3 - 4x + 1$ at $x = 2$. (5)



c) Express $e^{\sin x}$ in powers of x upto x^4 . (4)

Q-8 **Attempt all questions** (14)

a) State and prove Lagrange's mean value theorem. (5)

b) Apply Rolle's theorem for $f(x) = (x-1)\sin x$ in the interval $[0, 1]$ (5)

c) State Cauchy's mean value theorem also apply for $f(x) = x$ and $g(x) = x+1$ in $[1, 2]$. (4)

